

# Surface Splatting

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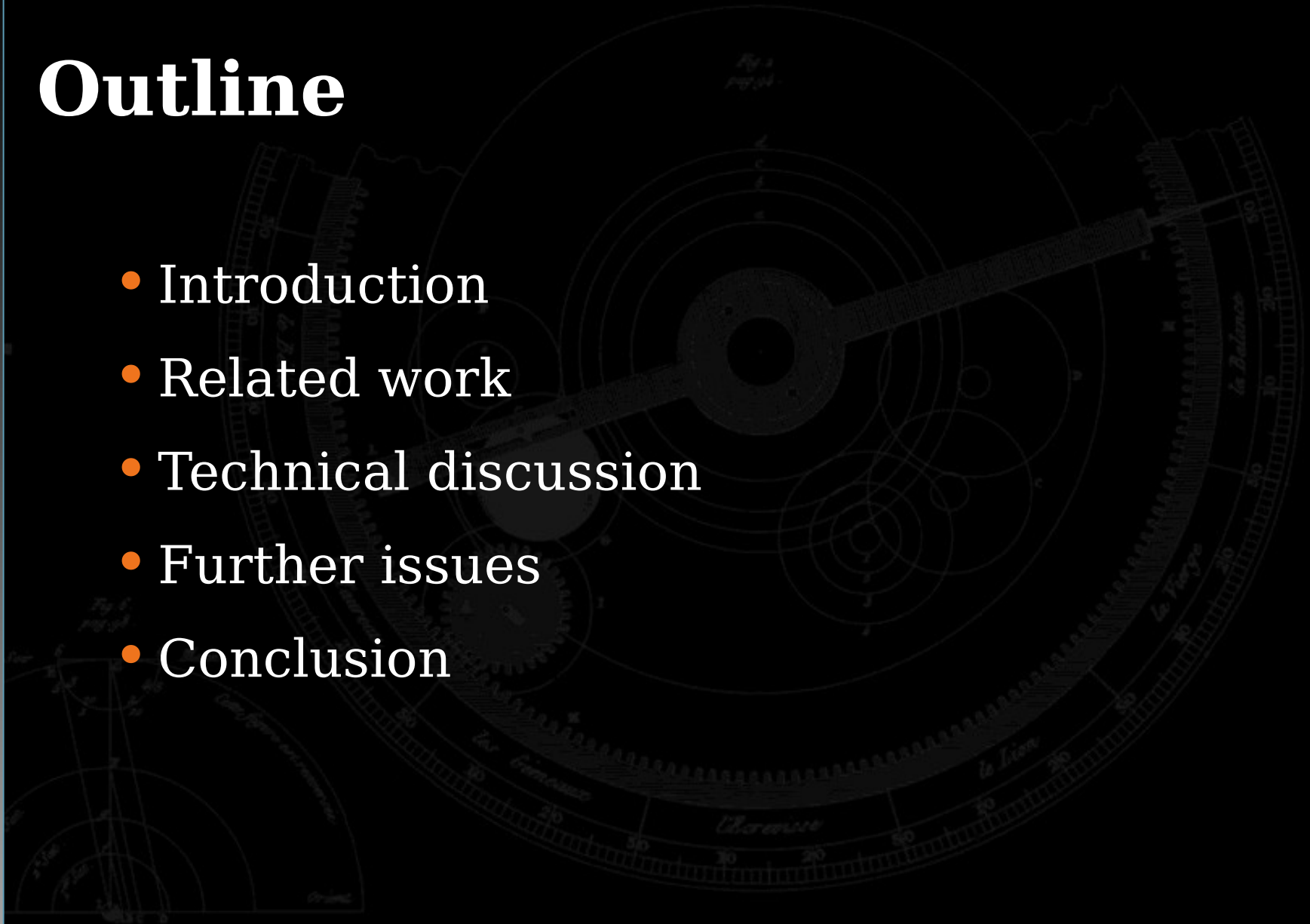


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Zurich**

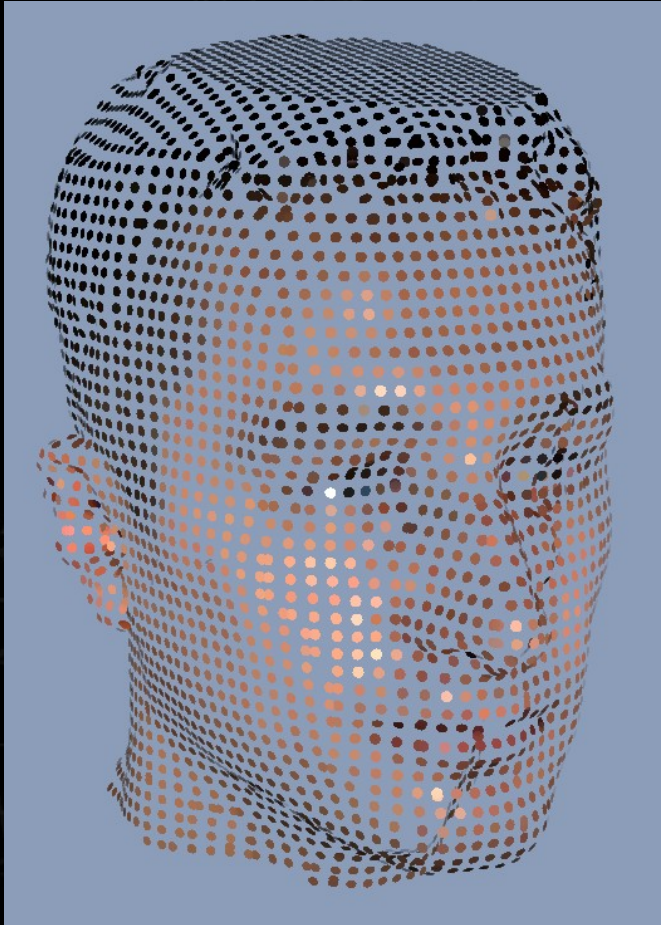


# Outline

- Introduction
- Related work
- Technical discussion
- Further issues
- Conclusion



# Point Rendering



- Surfaces are represented as a set of points without connectivity information
- Points store several surface attributes (*surfels*)
- To render, forward project each point separately

# Point vs. Polygon Rendering

## Points

- Efficient for highly complex models
- Fast preprocessing
- Ad hoc texture filtering and image reconstruction

## Polygons

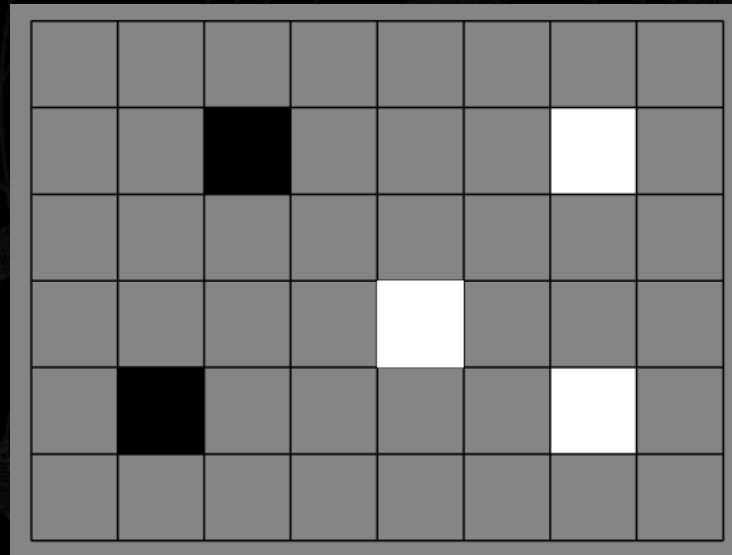
- Good for flat or slightly curved surfaces
- Costly mesh generation and LOD data structures
- High quality texture filtering algorithms available

# Image Reconstruction

- Generate a raster image from projected points
- Similar to polygon rasterization:  
*Sample projected rendering primitives at output pixel locations*
- Avoid sampling artifacts (holes, aliasing)

# Sampling Artifacts

screen space



*pixel sampling*



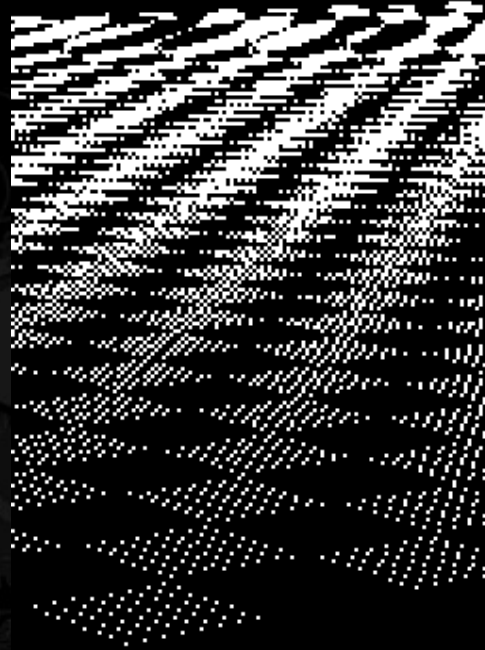
# Pixel Sampling

minification

aliasing

magnification

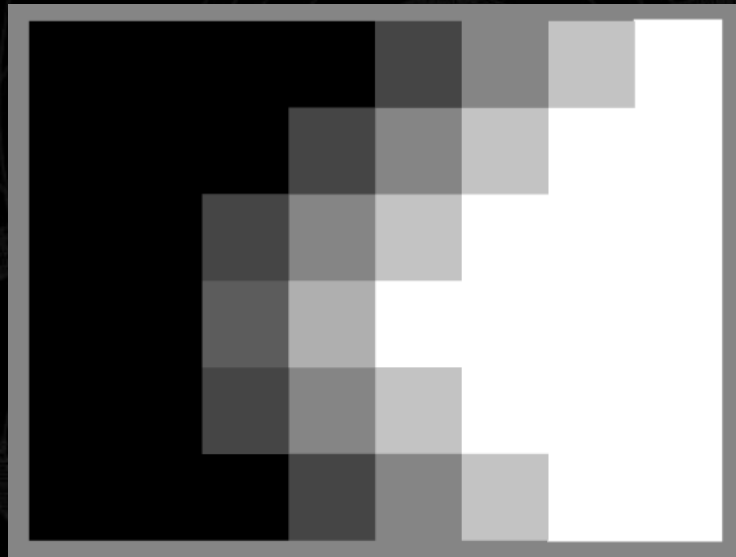
holes



128 x 192

# Splatting

screen space



*splatting*



# Splatting Comparison

*elliptical  
splats*

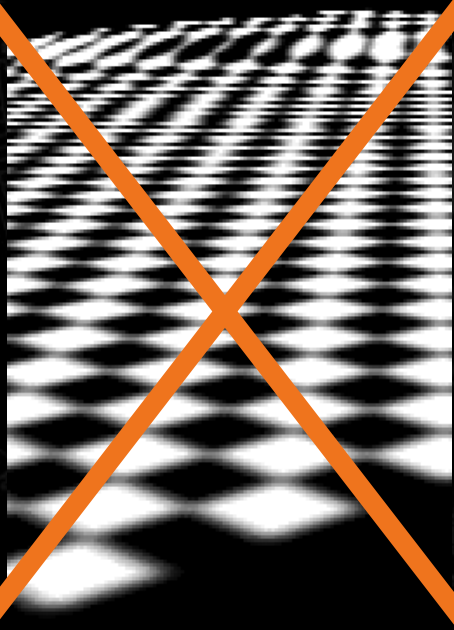
*circular  
splats*

*surface  
splatting*

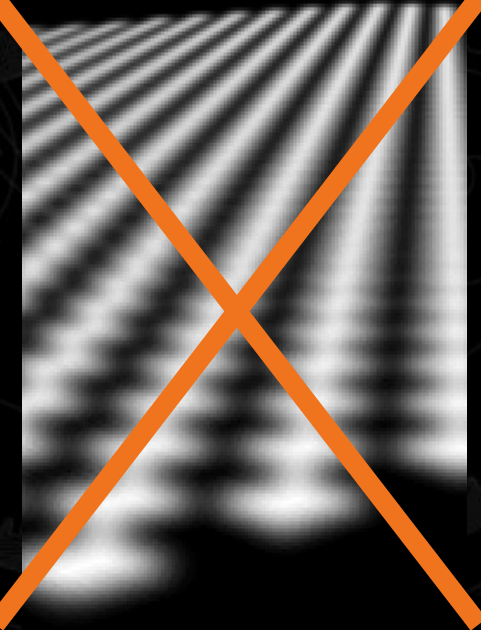
minif.



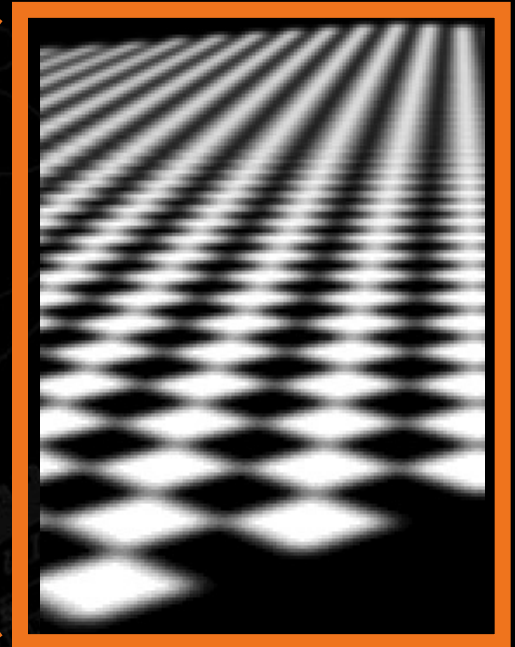
magnif.



128 x 192



128 x 192



128 x 192

# Related Work

## Point Rendering

- Levoy, Whitted 1985
- Rusinkiewicz, Levoy 2000
- Pfister et al. 2000

## Volume Rendering

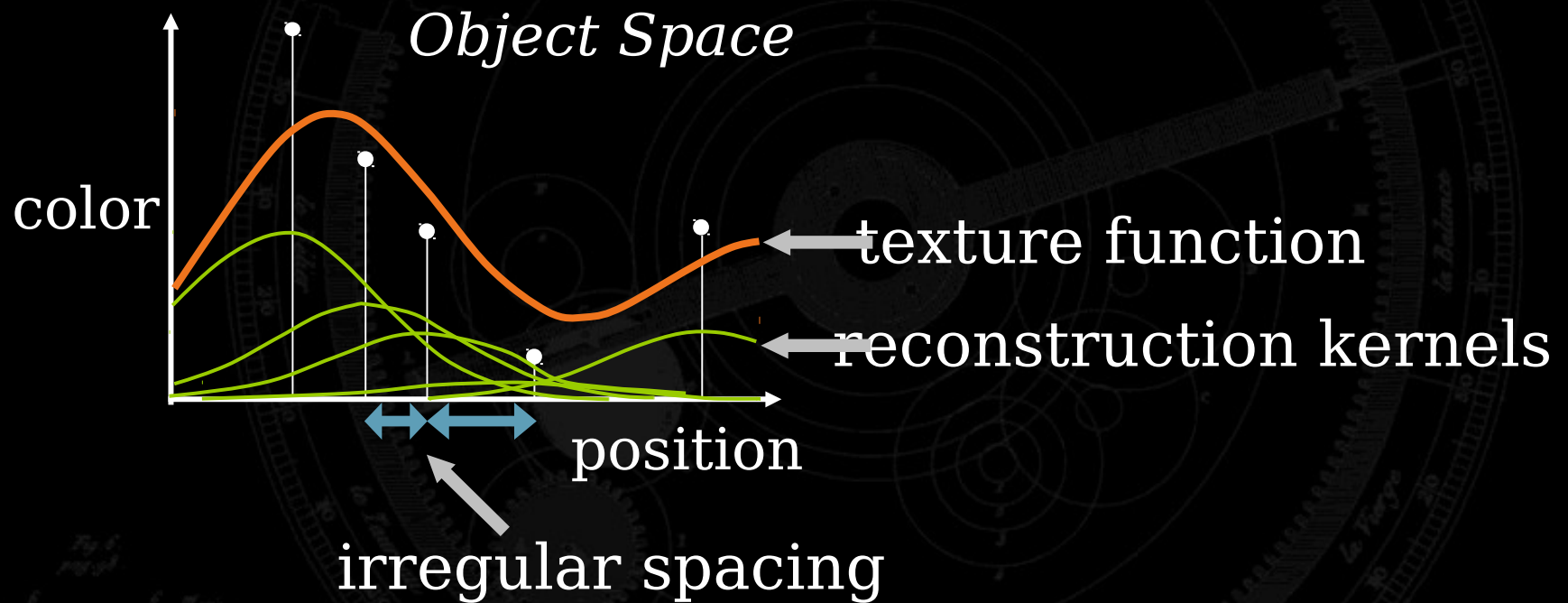
## Image-based Rendering

## Texture Mapping

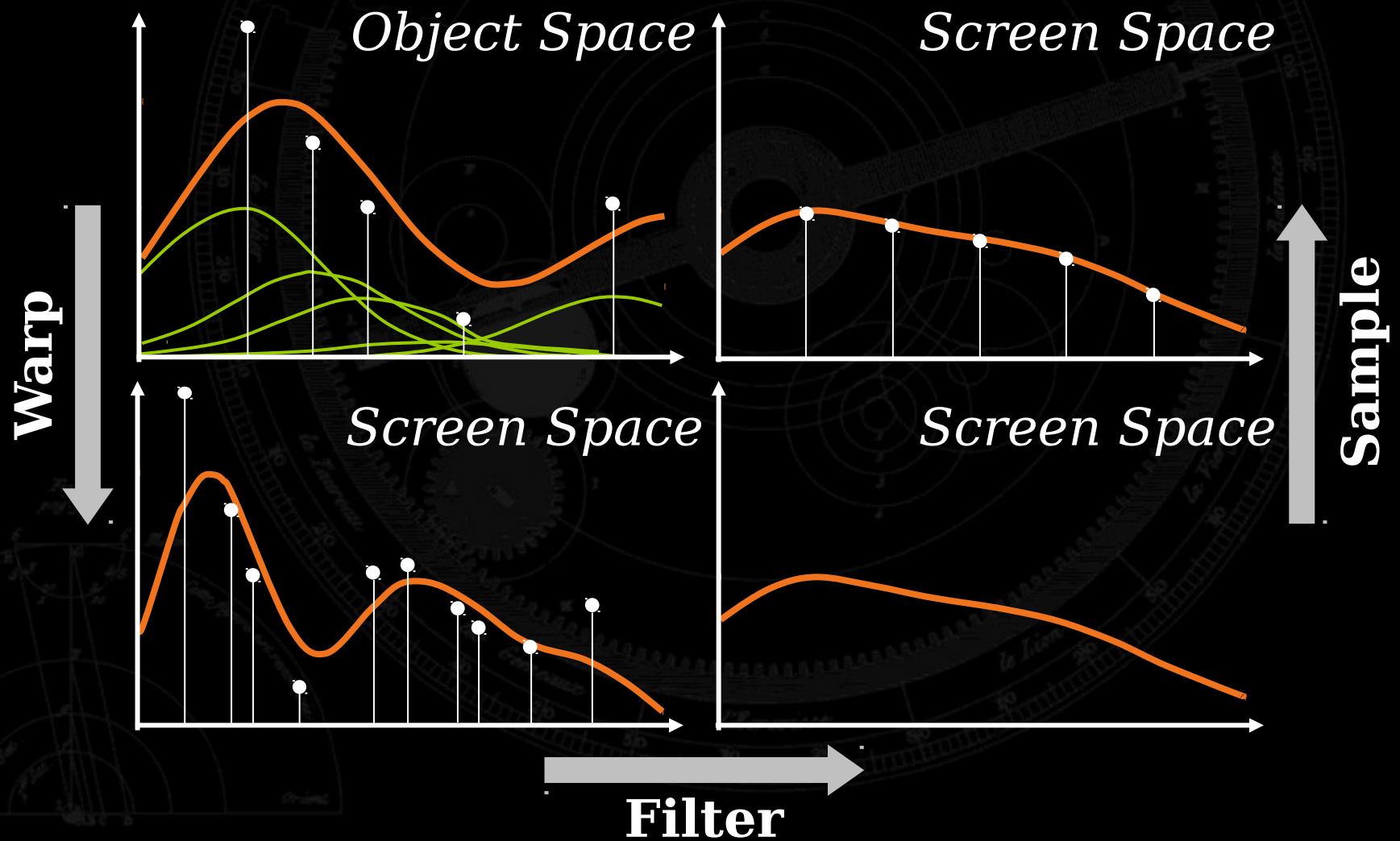
- Greene, Heckbert 1986
- Heckbert 1989  
*EWA texture filter*

**Surface Splatting**

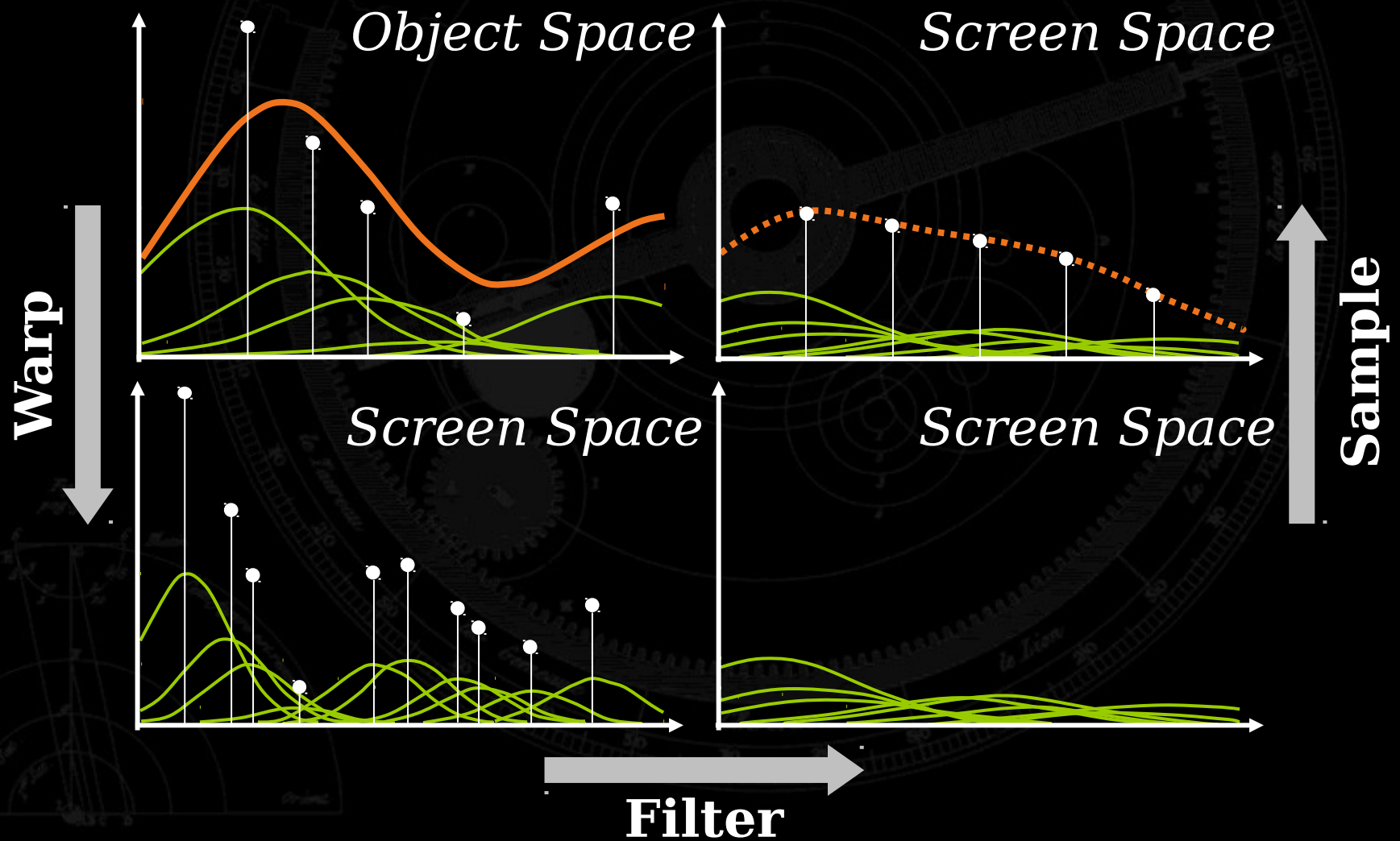
# The Surface Splatting Framework: 1D



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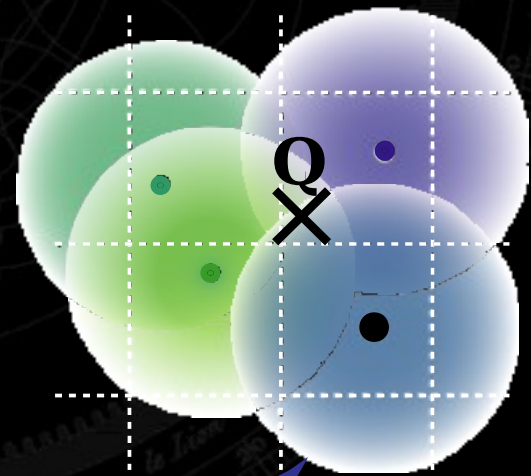
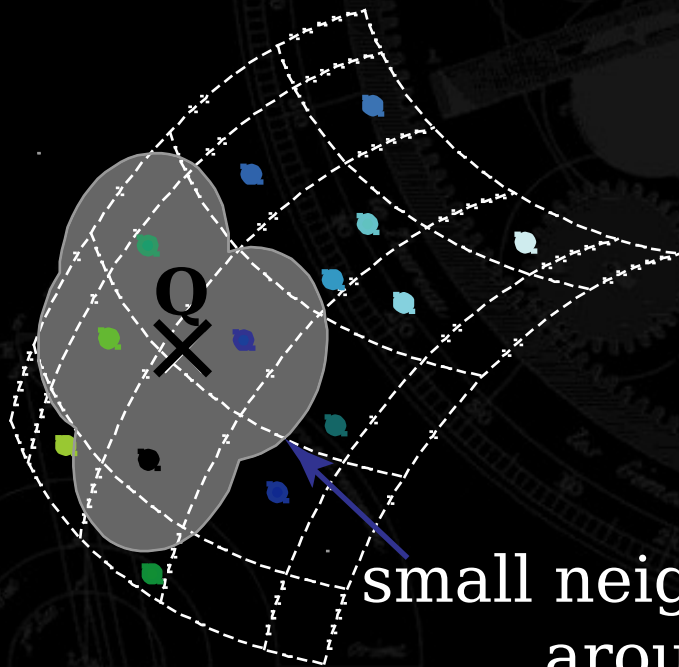
# 2D Texture Function

*local parameterization*



*3D object space*

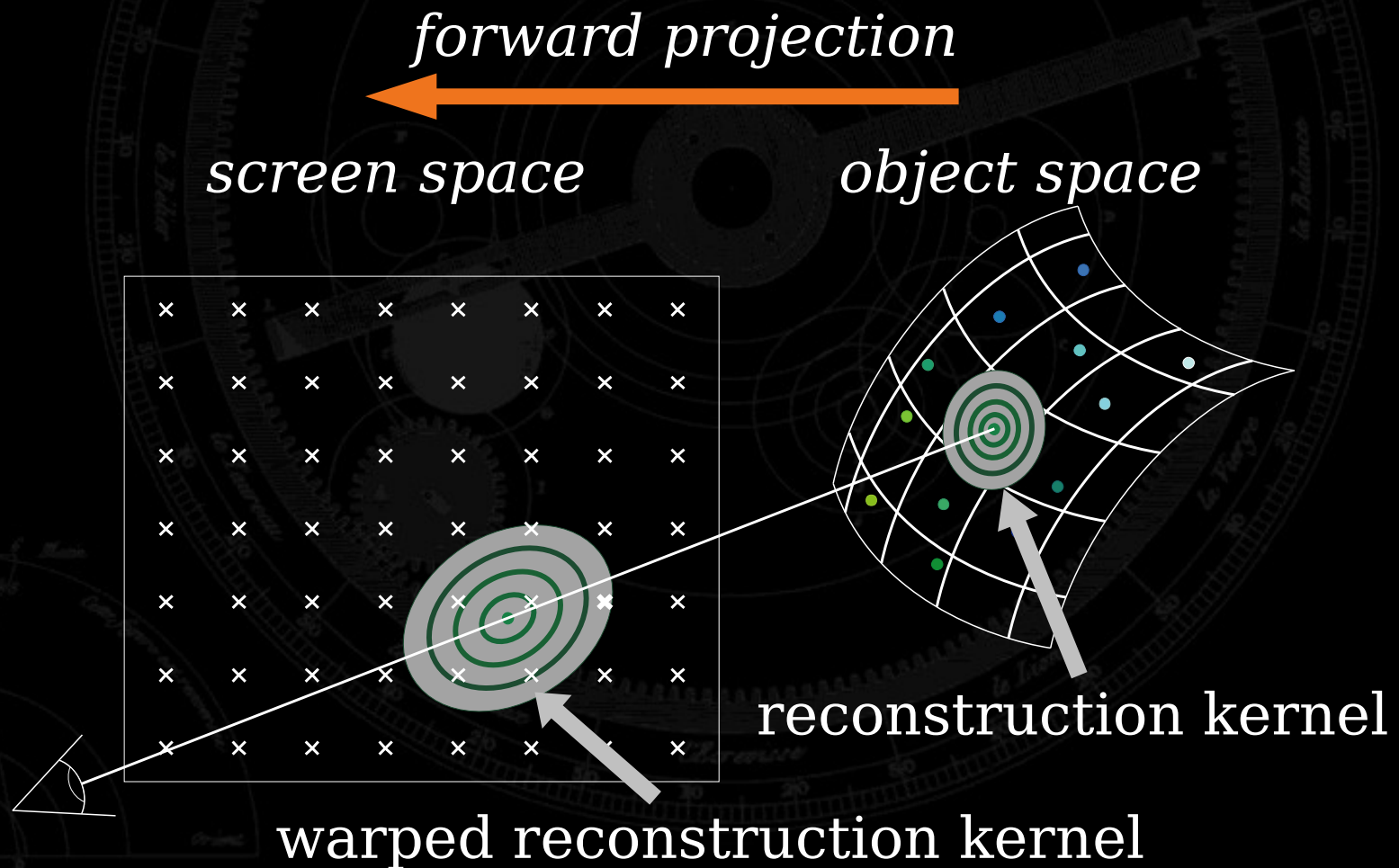
*2D parameterization*



small neighborhood reconstruction kernel  
around  $Q$

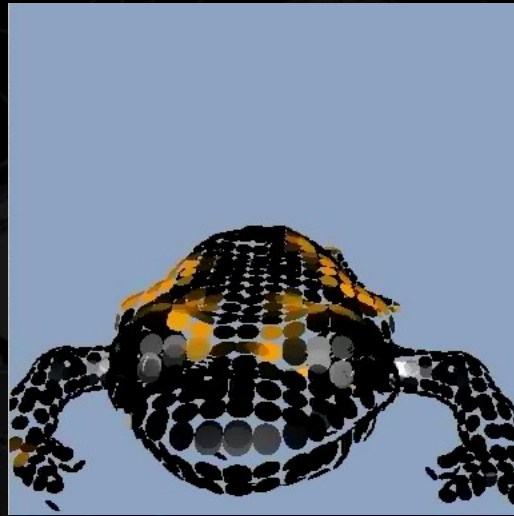


# Warping the 2D Texture Function





# Projecting the Reconstruction Kernels



# Mathematical Formulation

$$g(x) = \sum_k w_k r_k(m^{-1}(x)) \otimes h(x)$$

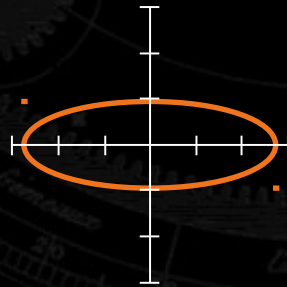
*screen space resampling filter*

- The *screen space* resampling filter combines a *warped reconstruction kernel* and a *low-pass filter*
- The *screen space* formulation is inverse to Heckbert's *source space* resampling filter

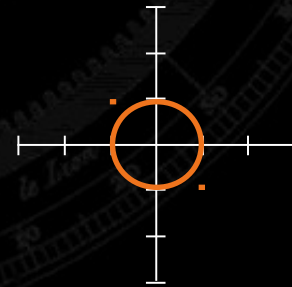
# Gaussian Kernels

$$g(x) = \sum_k w_k r_k(m^{-1}(x)) \otimes h(x)$$

Gaussian reconstruction kernel      Gaussian low-pass filter



*screen space*



*screen space*

# Gaussian Kernels

- Closed under affine mappings and convolution

$$g(x) = \sum_k w_k r_k(m^{-1}(x)) \otimes h(x)$$

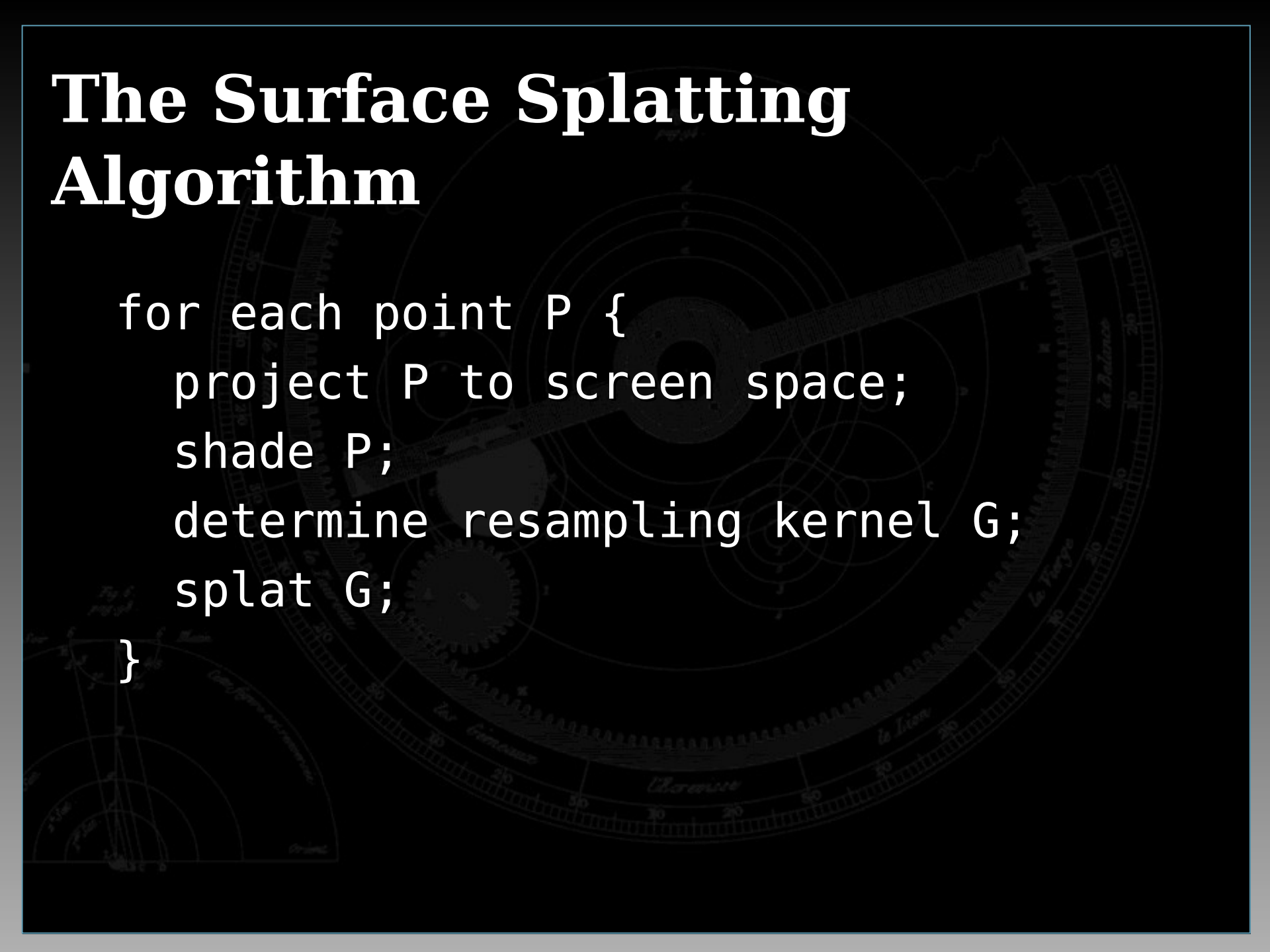
$$= \sum_k w_k G_k(x)$$

Gaussian resampling filter  
*“screen space EWA”*

- Analytic expression of the resampling filter can be computed efficiently

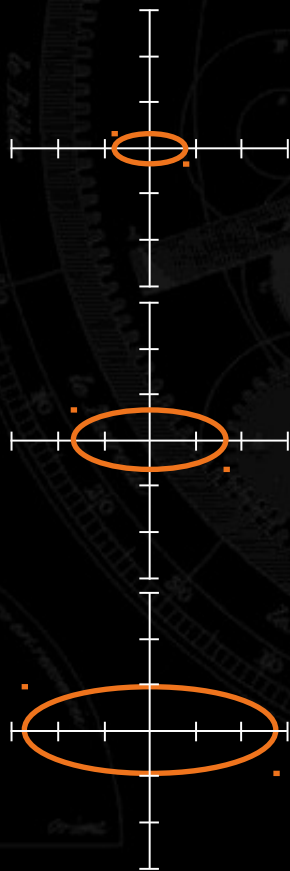
# The Surface Splatting Algorithm

```
for each point P {  
    project P to screen space;  
    shade P;  
    determine resampling kernel G;  
    splat G;  
}
```



# Reconstruction Kernel Only

reconstruction  
kernel



minification



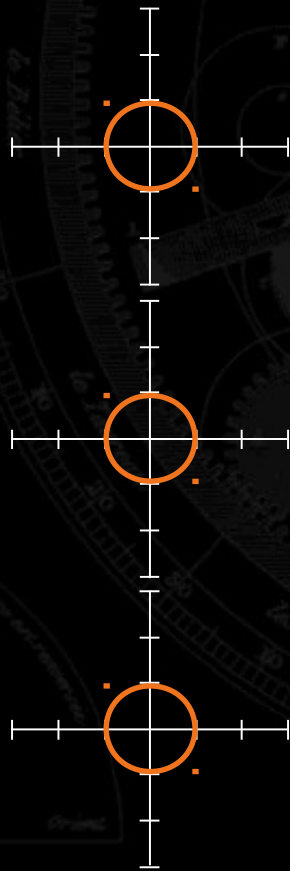
aliasing

smooth  
reconstruction

magnification

# Low-Pass Filter Only

low-pass  
filter



minification



no aliasing

holes

magnification



# Screen Space EWA

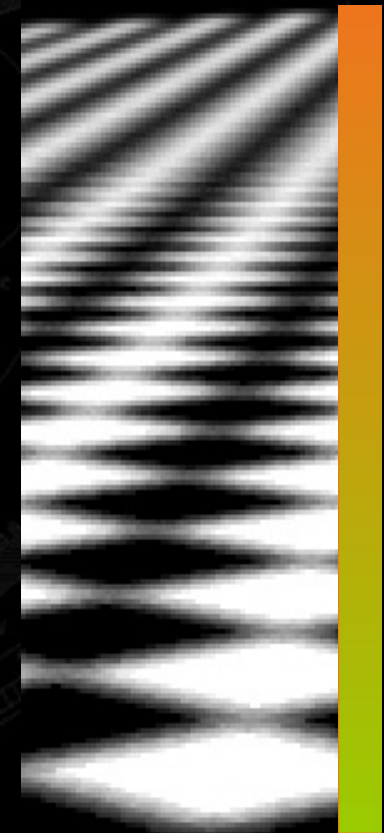
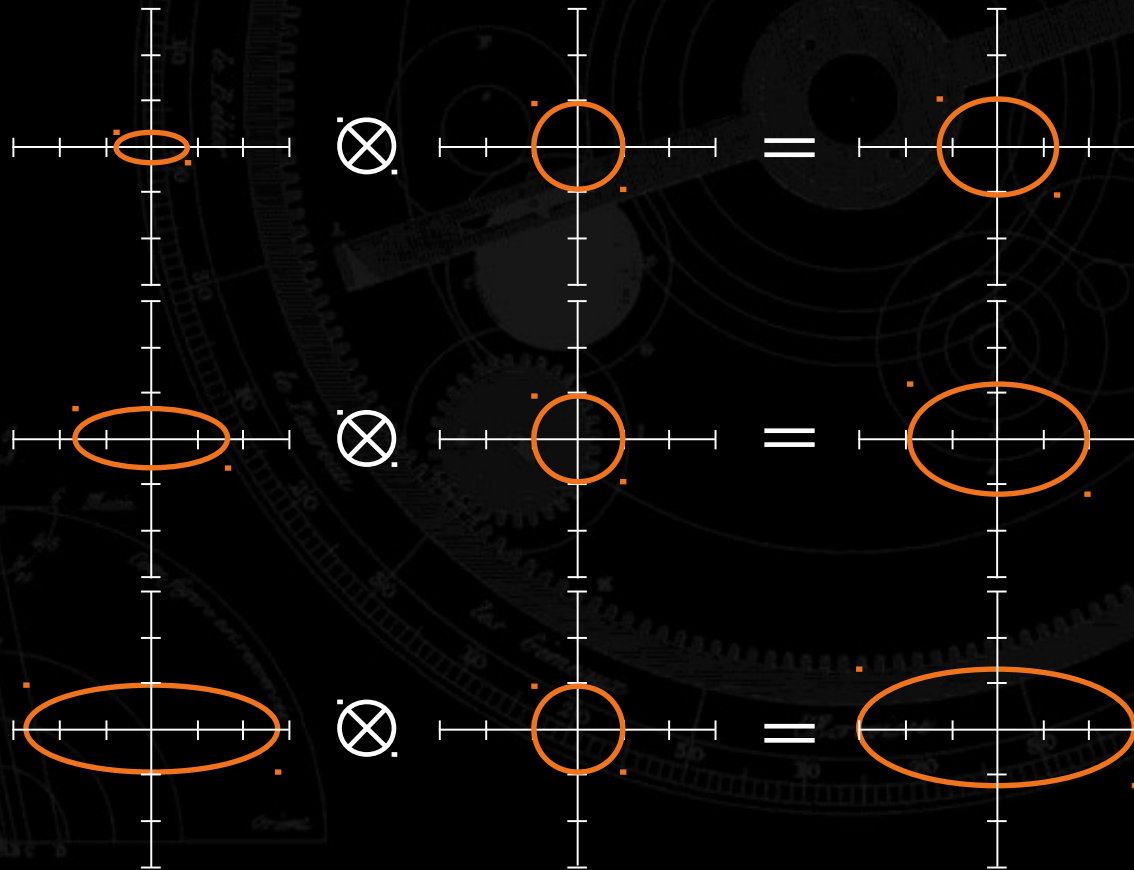
## Properties

warped reconstruction kernel

low-pass filter

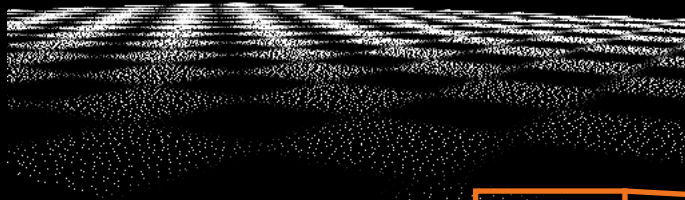
resampling filter

minification



magnification

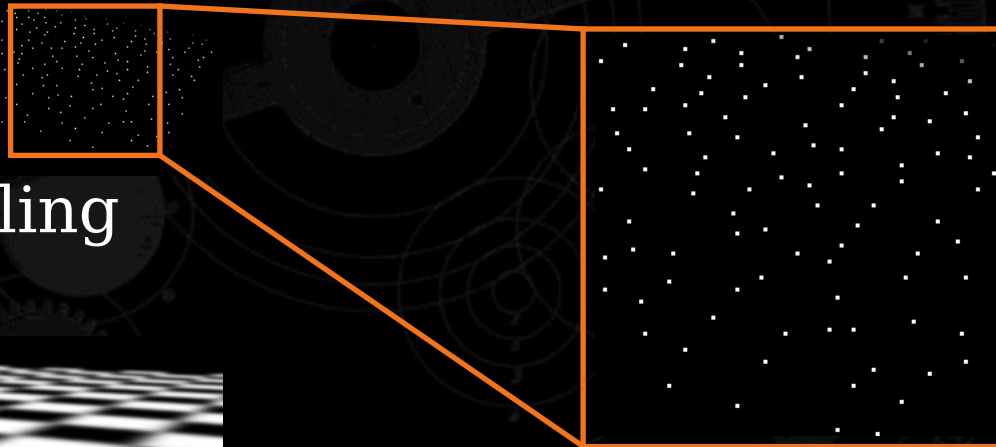
# Irregular Textures



pixel sampling



screen space EWA

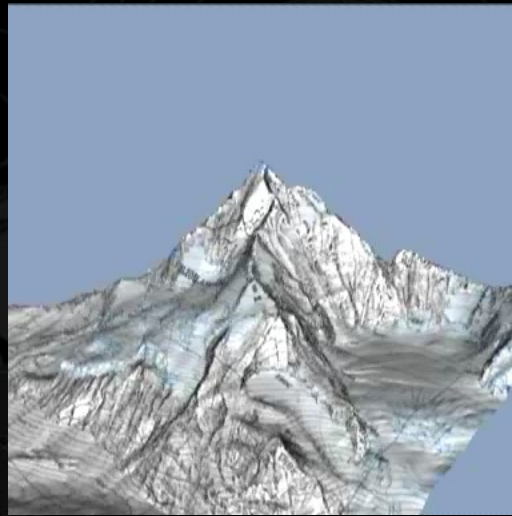


sampling pattern

# Filter Normalization

- In the irregular setting, the resampling kernels do not sum up to one
- Solution alternatives:
  - In a pre-process, optimize the weights such that normalization is not necessary
  - Perform per pixel normalization after sampling at the pixel centers

# Textured Digital Terrain

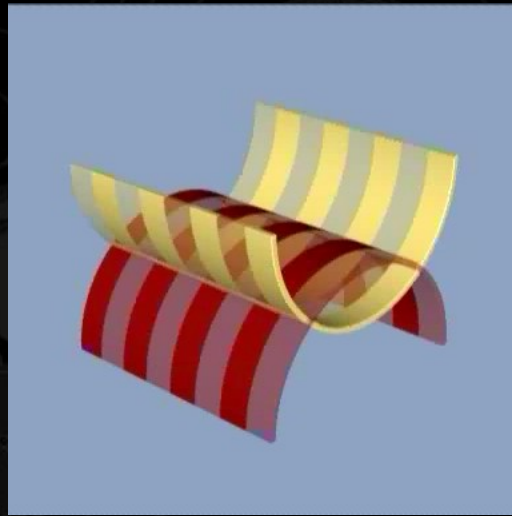


# Further Issues

- Mathematical formulation of the resampling filter
- Details of the surface splatting algorithm
- Texture acquisition, weight computation
- Rendering semi-transparent surfaces
- Edge antialiasing

# Semi-transparent Surfaces

## Edge Antialiasing



# Summary: Surface Splatting

- Point rendering method with high-quality image reconstruction
- Based on Paul Heckbert's EWA texture filter
- Anisotropic texture filtering for irregular point-sampled objects
- Transparency, edge antialiasing
- Can replace heuristics of previous splatting methods and provides superior texture quality



# Future Work

- Computation of Gaussian reconstruction kernels
- Scanned objects
- Compression
- Volume rendering (IEEE Visualization 2001)
- Hardware acceleration

# Acknowledgements

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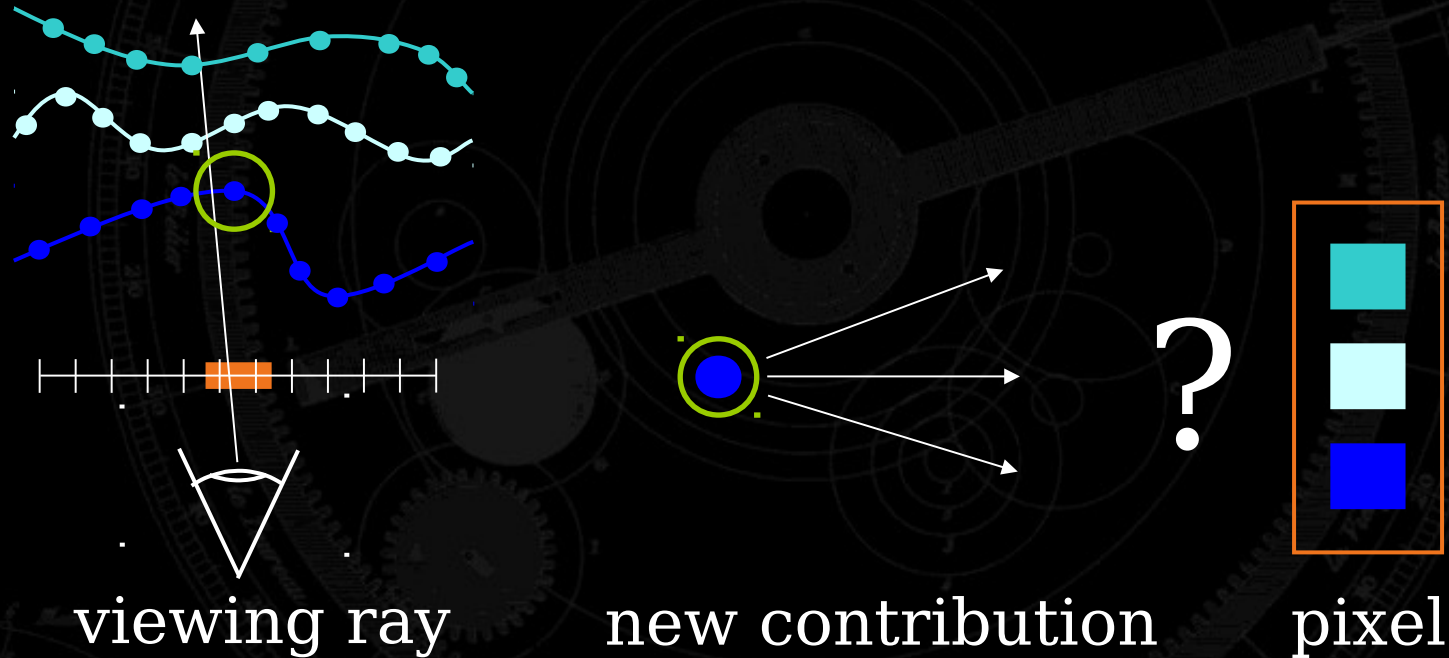
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# Transparency

- Use modified A-buffer algorithm
- Contributions of each surface are accumulated in a separate bucket
- Challenge is to correctly decide to which bucket a new contribution belongs

# Transparency



- Extrapolate depth on tangent plane
- Use depth comparisons to find correct bucket
- Blend buckets back-to-front